

# Principles of Communications

## ECS 332

**Dr. Prapun Suksompong**

[prapun@siit.tu.ac.th](mailto:prapun@siit.tu.ac.th)

## 7. Angle Modulation



**Office Hours:**

**BKD 3601-7**

**Monday 14:40-16:00**

**Friday 14:00-16:00**

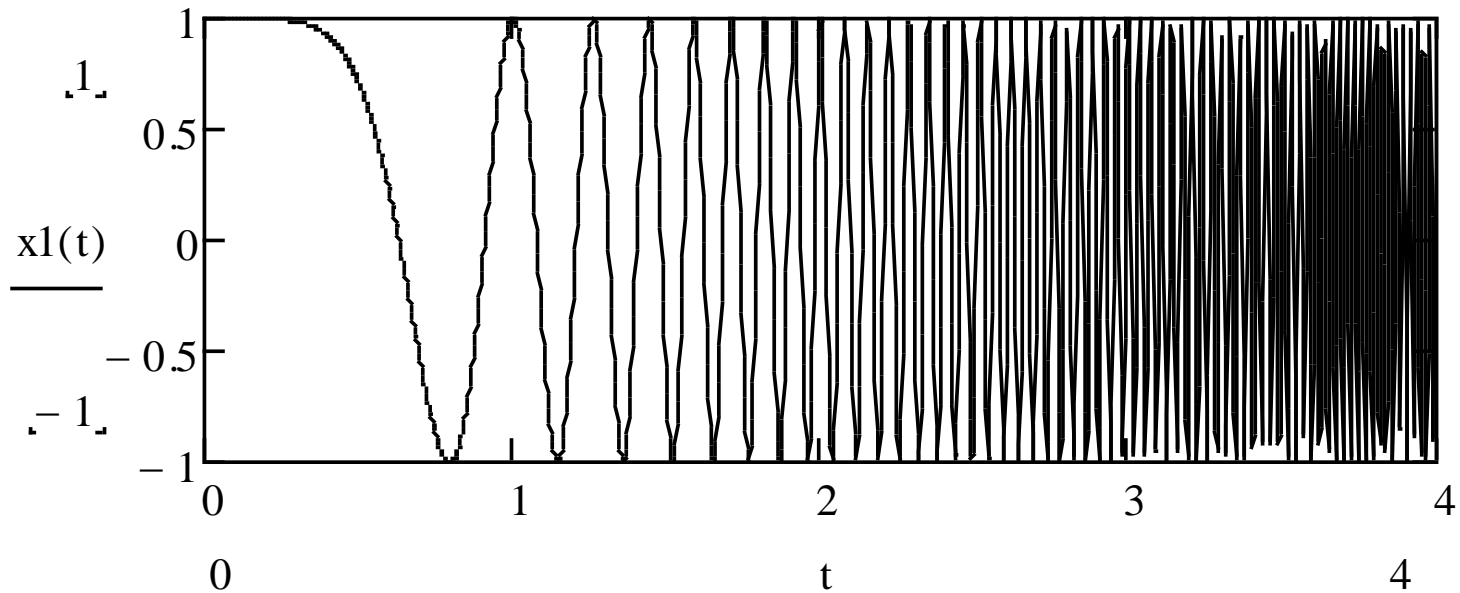
$$f(t) = t^2$$

# Instantaneous Frequency

$$\theta(t) = 2\pi t^3$$

$$x_1(t) = \cos(\underbrace{2\pi t^2}_\theta)$$

$$f(t) = \frac{2\pi \cdot 3t^2}{2\pi} = 3t^2$$

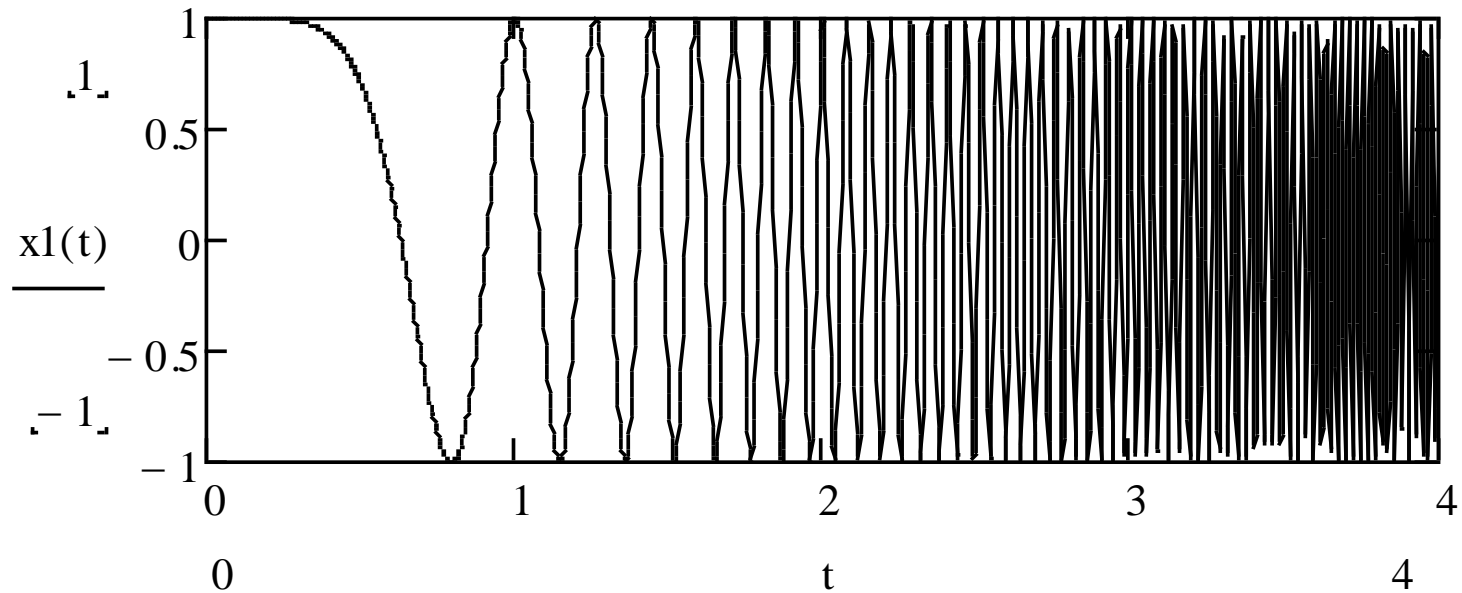


At  $t = 2$ , frequency = ?



# Instantaneous Frequency

$$x_1(t) = \cos(2\pi t^2 t)$$

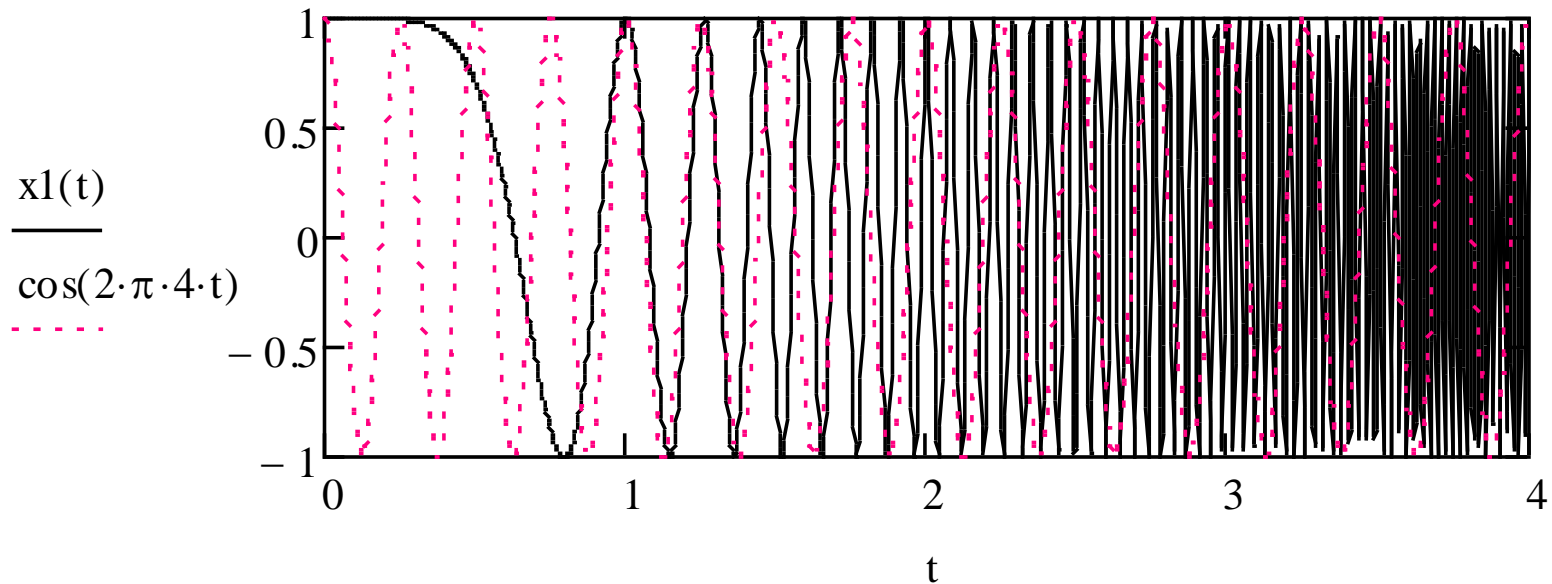


$\cos(2\pi ft)$   $\longrightarrow$  At  $t = 2$ ,  $f = t^2 = 4$  Hz?



# Instantaneous Frequency

$$x_1(t) = \cos(2\pi t^2 t)$$

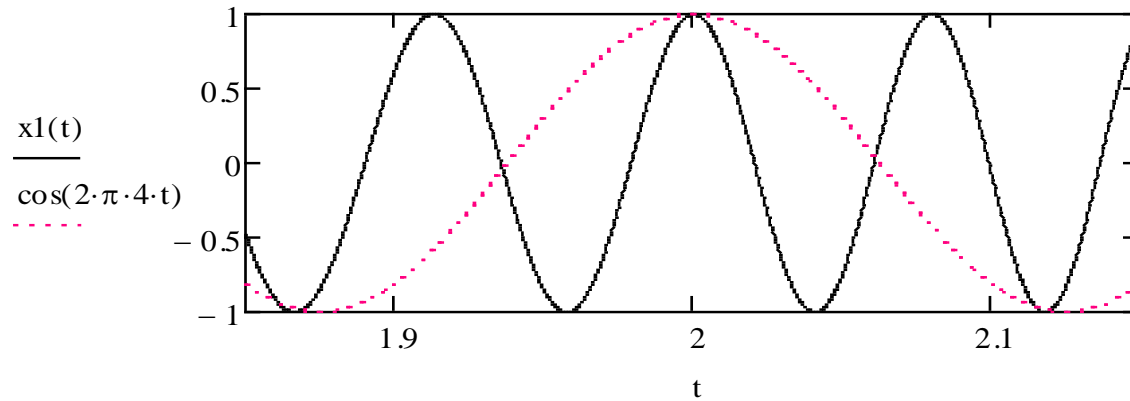
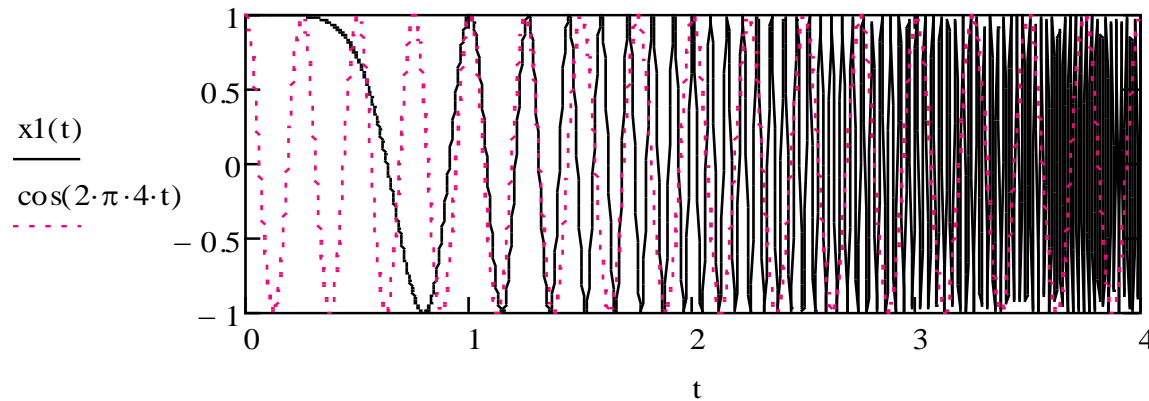


$\cos(2\pi ft)$   $\longrightarrow$  At  $t = 2$ ,  $f = t^2 = 4$  Hz?



# Instantaneous Frequency

$$x_1(t) = \cos(2\pi t^2)$$

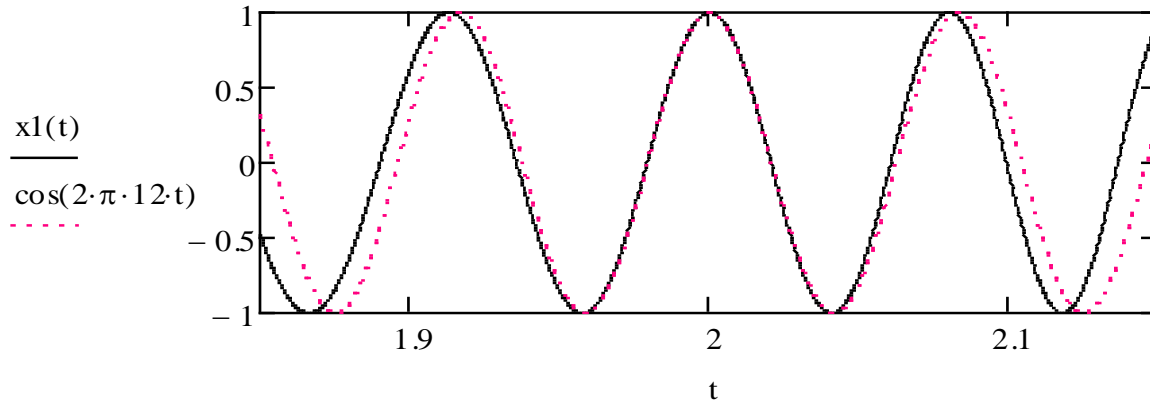
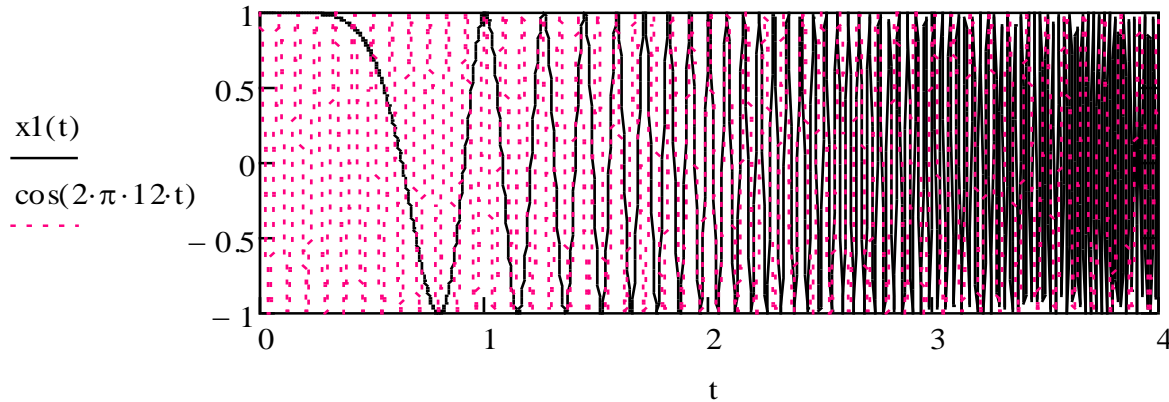


4 Hz is too low!!!



# Instantaneous Frequency

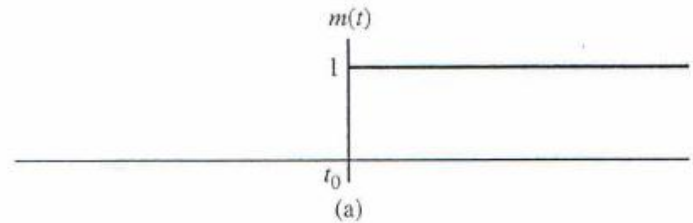
$$x_1(t) = \cos(2\pi t^2)$$



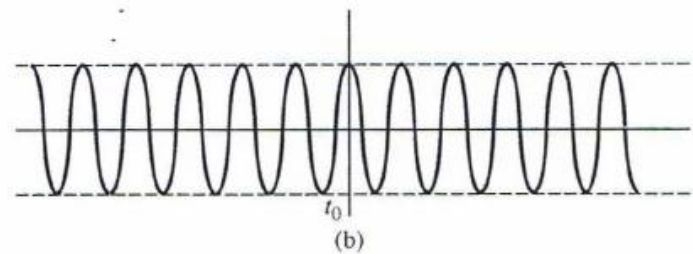
12 Hz?



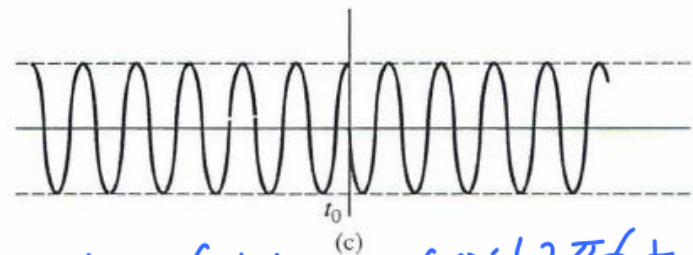
# FM vs. PM



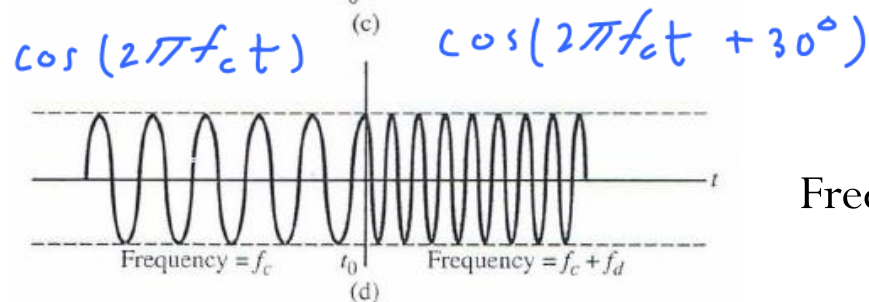
Message signal



Unmodulated carrier



Phase-modulated signal

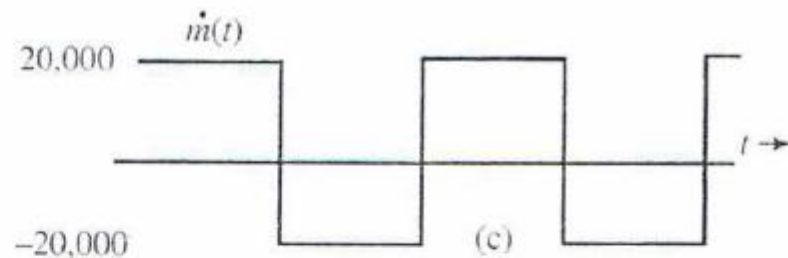
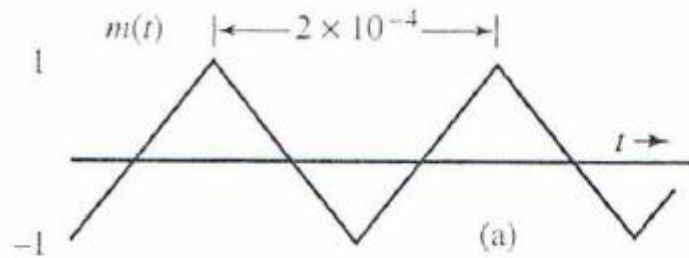


Frequency-modulated signal

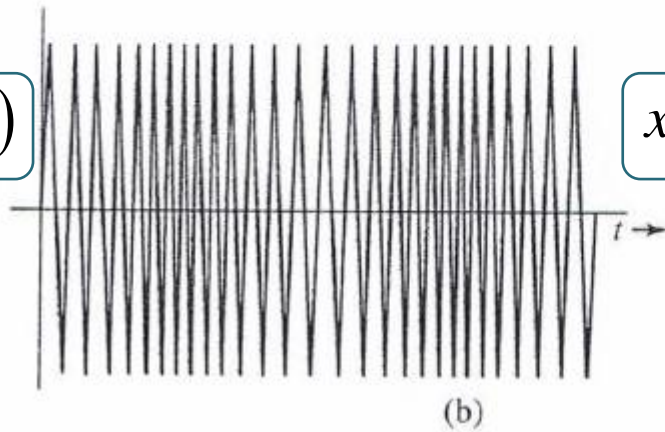


# FM vs. PM

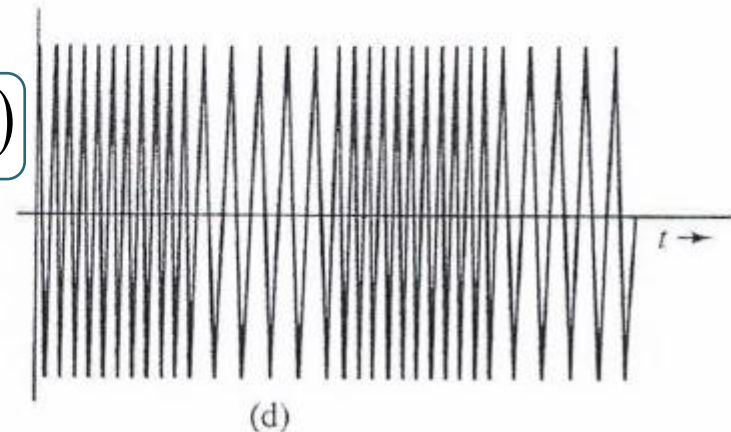
Remark: To see  $x_{PM}(t)$  of time varying  $m(t)$ , it is usually easier to look at the instantaneous freq. via the derivative first.



$x_{FM}(t)$

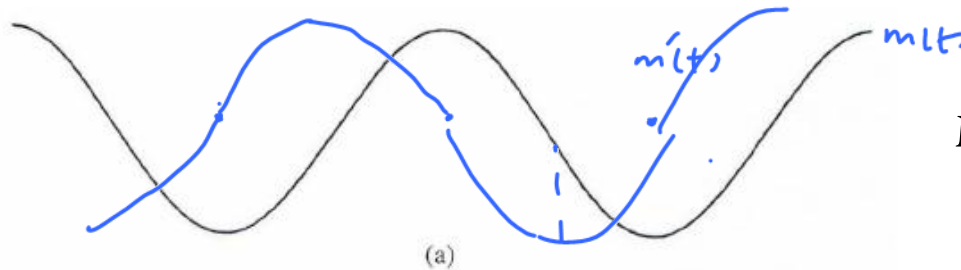


$x_{PM}(t)$

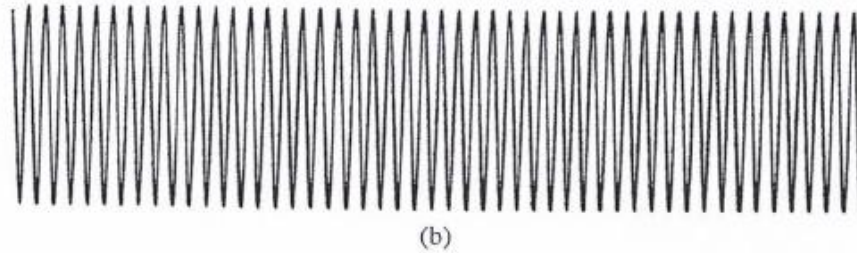




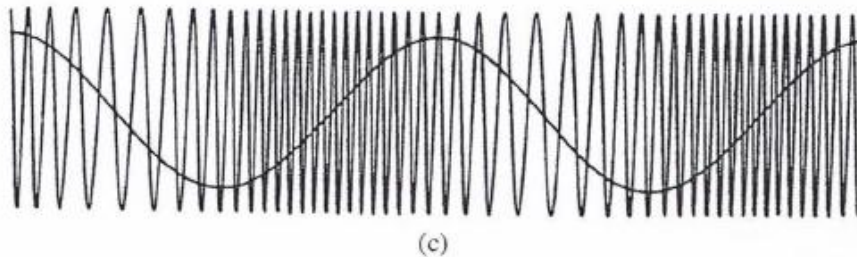
# FM vs. PM



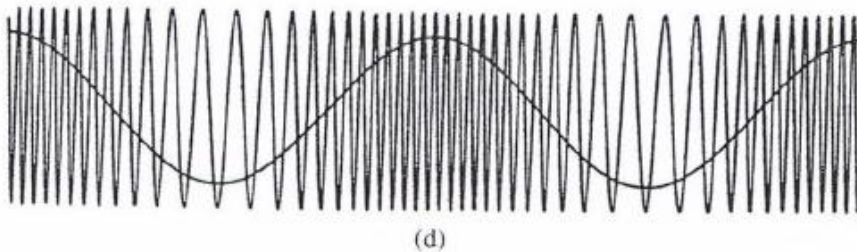
Message signal



Unmodulated carrier



Phase-modulated signal



Frequency-modulated signal

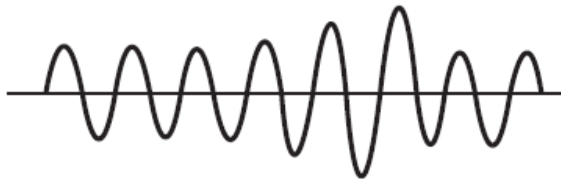


# AM, FM, and PM

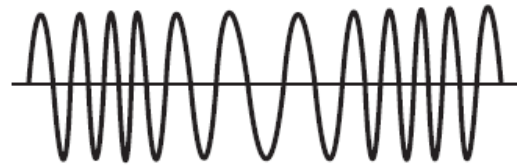
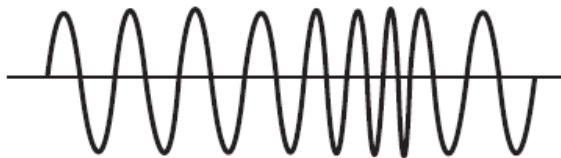
Modulating  
signal



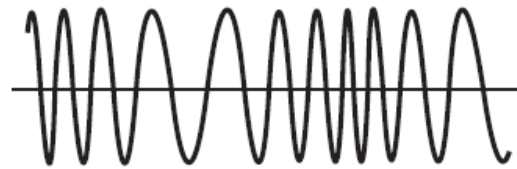
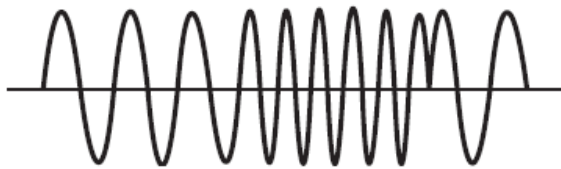
AM



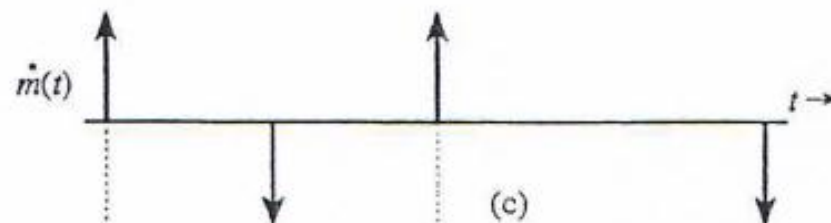
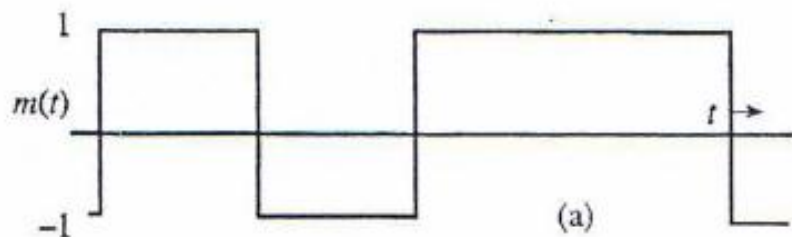
FM



PM



# FM vs. PM

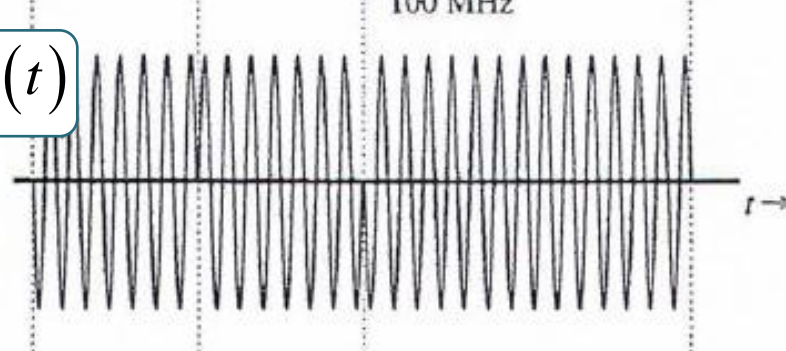
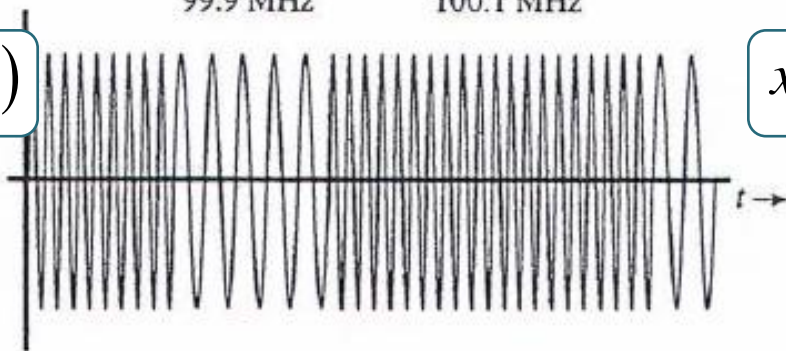


99.9 MHz      100.1 MHz

100 MHz

$x_{FM}(t)$

$x_{PM}(t)$



(b)

(d)

